

Can Thin Film Alloy Refractive Index Be Accurately predicted?

---Theoretical & Experimental Study Thin Film Alloy AgZn Refractive Index

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Abstract

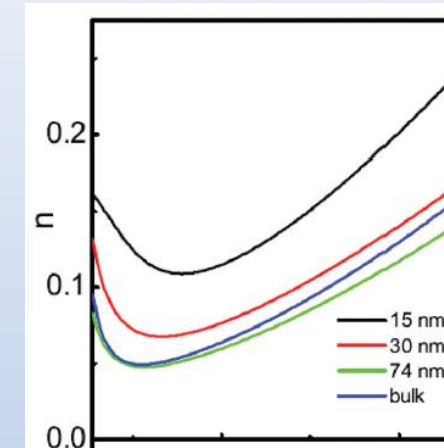
- The optical refractive index and electrical resistivity ρ of Silver Zinc alloy were studied experimentally by a co-sputtering method.
- Currently, the theories on alloys refractive index are too complex, dependent on too many factors, so it can still only be a semi-practical prediction.
- In this study, a new theoretical method was developed to simplify the calculation of silver alloy IR refractive index, and also valid experimental condition was found.
 - (1) Theoretically, the refractive index ratio $n_{\text{alloy}}/n_{\text{Ag}}$ between silver and its alloy at IR region is derived, a way to cancel out most factors so that it only depends on free electron density n_e and the film resistivity ρ
 - (2) Experimentally, this assumption was approximately met at a special conditions
 - (3) The experimental results agreed well with this simplified calculation.
- Further how the zinc electrons contribute to the optical and electrical properties in low Zn concentration AgZn alloy (<10%) was experimental presented and discussed in this study.

Introduction

- We are initially curious
 - Why are there no accurate theory calculations for metal thin film refractive index?
- Can we derive such an accurate theoretical calculation?
- Can we prove the theory by experiments?

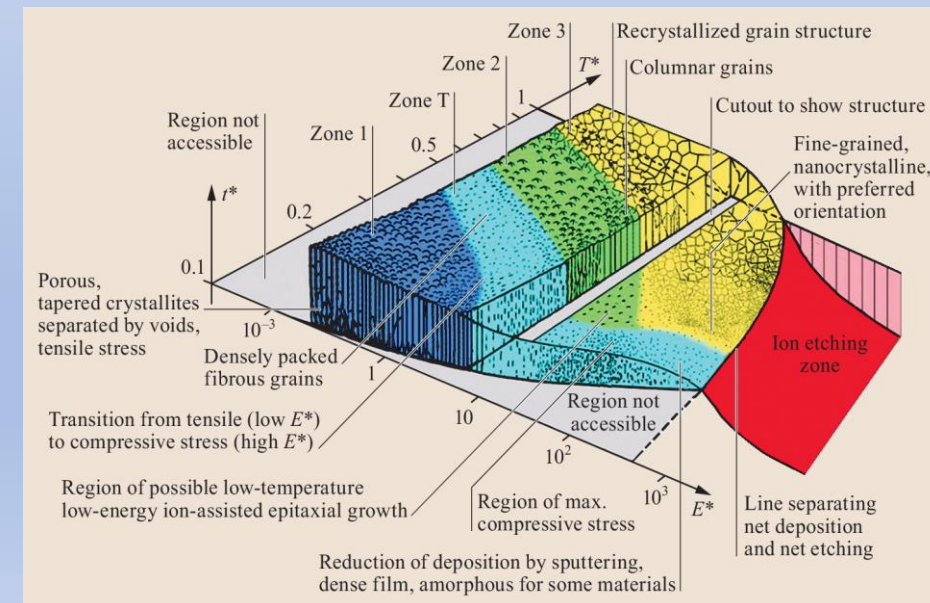
Why refractive index calculation is hard to meet thin film value

- The thin film refractive index is dependent on too many factors,
 - up to multiple hundred % impacting on the index
- Complexity physics for thin film alloys optical and electrical properties
 - Alloy Atom structure, Crystal or amorphous/Crystal structure
 - Crystal defects/ Materials impurity
 - Film thickness / roughness / Grain size
 - Substrate materials
 - Ambient environmental conditions (temperature, humidity, queue time)
 - Deposition condition: pressure/ temperature / power / gun to substrate distance/...



Ref. 3
silver thin film
refractive index
varied more than 2
times

Thornton diagram: thin film properties varied significantly as different deposition conditions



Theory on metal properties calculation

Free electron model Assumption: (function of X , E (electric field), ω (frequency), τ (collision time))

Dielectric Constant ϵ_r definition
(function of X , E)

Dielectric Constant ϵ_r is
function of ω , τ , ω_{pe} frequency,
collision time, plasma frequency, which is
function of electron density (n_e)

optical and electric properties

More
In detail

- Drude-Lorentz Model assumptions: (widely used, especially for group I and XI elements)

- In math: $-eE(t) = m_e \frac{d^2x}{dt^2} + \frac{m_e}{\tau} \frac{dx}{dt}$ (1)

- The Solution is $X = \frac{eE}{m_e(\omega^2 + i\frac{\omega}{\tau})}$ (2)

- The electric displacement field: $D \equiv \epsilon_0 E + P \equiv \epsilon_r \epsilon_0 E$ (3)

- And polarization $P = -e \cdot n_e x$ (4)

- Substitute Eqs.(2),(4) into Eq. (3) \rightarrow
dielectric constant $\epsilon_r = 1 - \frac{\omega_{pe}^2}{\omega^2 + i\frac{\omega}{\tau}} = 1 - \frac{\omega_{pe}^2 \tau^2}{1 + \omega^2 \tau^2} + i \frac{\omega_{pe}^2 \tau^2}{\omega \tau (1 + \omega^2 \tau^2)}$ (5)

Where ω_{pe} is plasma frequency, $\omega_{pe}^2 = \frac{n_e e^2}{\epsilon_0 m_e}$ (6)

- And Ohm's & Newton's laws \rightarrow Collision time $\frac{1}{\tau} = \frac{n_e e^2 \rho}{m_e}$ (7)

e: is electron charge
 m_e is electron mass
 τ : is the collision time
 ω : is frequency
 ω_{pe} : is plasma frequency
 n_e is electron density
 E : electric field
 D : electric displacement field
 P : polarization
 ϵ_0 : is dielectric Constant in vacuum
 ϵ_r : is relative dielectric Constant
 ϵ_1 : is real part of dielectric Constant
 ϵ_2 : is imaginary part of ϵ_r
 ρ : is resistivity

Refractive Index calculation was simplified from literatures

- Refractive index mathematically

$$n + ik = \sqrt{\epsilon_r} = \sqrt{\epsilon_1 + i\epsilon_2}$$

Calculation Eq(5) can be simplified by

- Assumption 2:** $|\epsilon_1| \gg |\epsilon_2|$;

– Valid for group 1 and 11

- Assumption 3:** $\omega^2 \tau^2 \gg 1$;

– Valid for wavelength $< 3\mu m$

→ index n is function of

– Electron density n_e

– Resistivity ρ ,

– Frequency ω

$$\epsilon_r = 1 - \frac{\omega_{pe}^2}{\omega^2} + i \frac{\omega_{pe}^2}{\omega^3 \tau} \quad (15)$$

$$n = \frac{n_e^2 e^4}{\epsilon_0 m_e^2} * \rho * \frac{1}{2k\omega^3} \quad (16)$$

Group	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
1	1 H																	2 He
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
6	55 Cs	56 Ba *	71 Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn

n is common refractive index
 k is extinction coefficient
 e : is electron charge
 m_e is electron mass
 n_e : is electron density
 ϵ_0 : is dielectric Constant in vacuum
 ρ : is resistivity

Develop a method for index calculation with two factors

- **Further simplification by an assumption 4: $\omega_{pe}^2 \gg \omega^2$**

- valid for wavelength > 0.6 μm

- ϵ_r can be simplified as Eq. 17, then substitute Eq. 18 into Eq. 16

$$\epsilon_r = -\frac{\omega_{pe}^2}{\omega^2} + i\frac{\omega_{pe}^2}{\omega^3\tau} \quad (17)$$

$$k = \sqrt{|\epsilon_1|} = \sqrt{\frac{\omega_{pe}^2}{\omega^2}} = \frac{\sqrt{\epsilon^2 n_e}}{\epsilon_0 m_e \omega} \quad (18)$$

- **Ratio \rightarrow cancel out most factors in index calculation**

Index ratio

$$\frac{n_{alloy}}{n_{Ag}} = \frac{n_{e-alloy}^{3/2} * \rho_{alloy}}{n_{e-Ag}^{3/2} * \rho_{Ag}} \quad (21)$$

$$\text{silver index } n_{Ag} = \frac{n_{e-Ag}^{1.5} e^3}{2\sqrt{\epsilon_0} m_e^{1.5} \omega^2} * \rho_{Ag} \quad (19)$$

$$\text{alloy index } n_{Alloy} = \frac{n_{e-Alloy}^{1.5} e^3}{2\sqrt{\epsilon_0} m_e^{1.5} \omega^2} * \rho_{alloy} \quad (20)$$

only dependent on two factors n_e and ρ , (free electron density and resistivity), with all other factors being cancelled out: (Assumption 5)

n_{Ag} : is silver index
 n_{Alloy} : is alloy index
 ρ_{Ag} : is silver resistivity
 ρ_{alloy} : is alloy resistivity
 n_{e-ag} : is silver electron density
 $n_{e-alloy}$: is alloy electron density

- **Can experiments be valid for these two factors? Yes, under special conditions**

- The Ag and AgZn alloy with low Zn concentration (<10%): The alloy co-sputter deposition conditions nearly identical to Ag's condition, except the alloy having an additional tiny Zinc co-sputtering power.

Derive thin film alloy refractive index calculation

- The alloy index can be calculated by n_e and ρ (eq. 21)
- Electron densities n_e of alloys have 2 possibilities
 - Zn atoms contributes 0 free electrons;

$$\text{Alloy Index } n_{\text{alloy}} = (1 - \text{Zn}\%)^{3/2} * \frac{\rho_{\text{alloy}}}{\rho_{\text{Ag}}} * n_{\text{Ag}} \quad (23)$$

- Each Zn atom contributes 2 free electrons;

$$\text{Alloy Index } n_{\text{alloy}} = (1 + 1.24\text{Zn}\%)^{3/2} * \frac{\rho_{\text{alloy}}}{\rho_{\text{Ag}}} * n_{\text{Ag}} \quad (25)$$

- Experiments can tell which is the correct one
- The alloy index can be accurately predicted if Ag index, Ag-Alloy resistivity and concentration are known

electron density calculation

$$\text{Alloy electron density } n_{e_{\text{alloy}}} = (1 - \text{Zn}\%)n_{e_{\text{Ag}}}$$

Alloy electron density:

$$\begin{aligned} n_{e_{\text{alloy}}} &= (1 - \text{Zn}\%)n_{e_{\text{Ag}}} + 2 * \text{Zn}\% * n_{e_{\text{Zn}}} \\ &= (1 - \text{Zn}\%) n_{e_{\text{Ag}}} + 2 * \text{Zn}\% \left(\frac{7.13}{10.49} \frac{107.87}{65.38} n_{e_{\text{Ag}}} \right) \end{aligned}$$

$n_{e_{\text{Zn}}}$ is transferred to $n_{e_{\text{Ag}}}$ by

the molecular weight and density conversion

Where Zn% is the volume percentage of Zn in the alloy

Silver molecular weight: 107.87 u

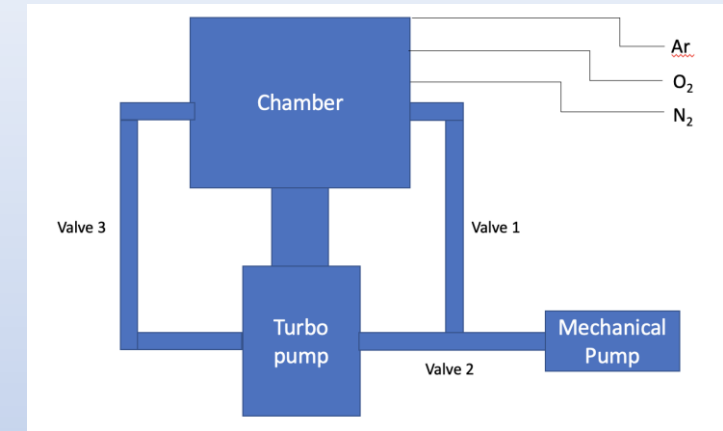
Zinc molecular weight: 65.38 u

Silver density: 10.49 g/cm³

Zinc density: 7.13 g/cm³

Experiment Setup

- PVD
 - Background vacuum: 2×10^{-7} torr
 - Ag and Zn target materials are 99.99%
 - Co-sputter to generate Ag Zn alloy
 - Pulsed DC (40kHz) power supply
- UV-VIS-IR Spectrometer (Shimadzu 3700)
 - 300-2500 nm spectra
 - Double beams, 3 sensors
 - Error bar is 0.2%
- Spectroscopic Ellipsometer (Woollam VASE)
 - 300-1700 nm
 - 3 measurement parameter (Delta, Psi, transmission)
 - Thickness accuracy 0.1 nm
- Four Point Probe
 - Accuracy 0.04 ohm



Zn contributes free electrons in alloy AgZn properties or not?

- If each Zn atom contributes 2 free electrons in alloy properties

$$\frac{n_{alloy}}{n_{Ag}} / \frac{\rho_{alloy}}{\rho_{Ag}} = (1 + 1.24Zn\%)^{3/2} \quad \times \quad (25)$$

- If each Zn atom contributes 0 free electrons in alloy properties

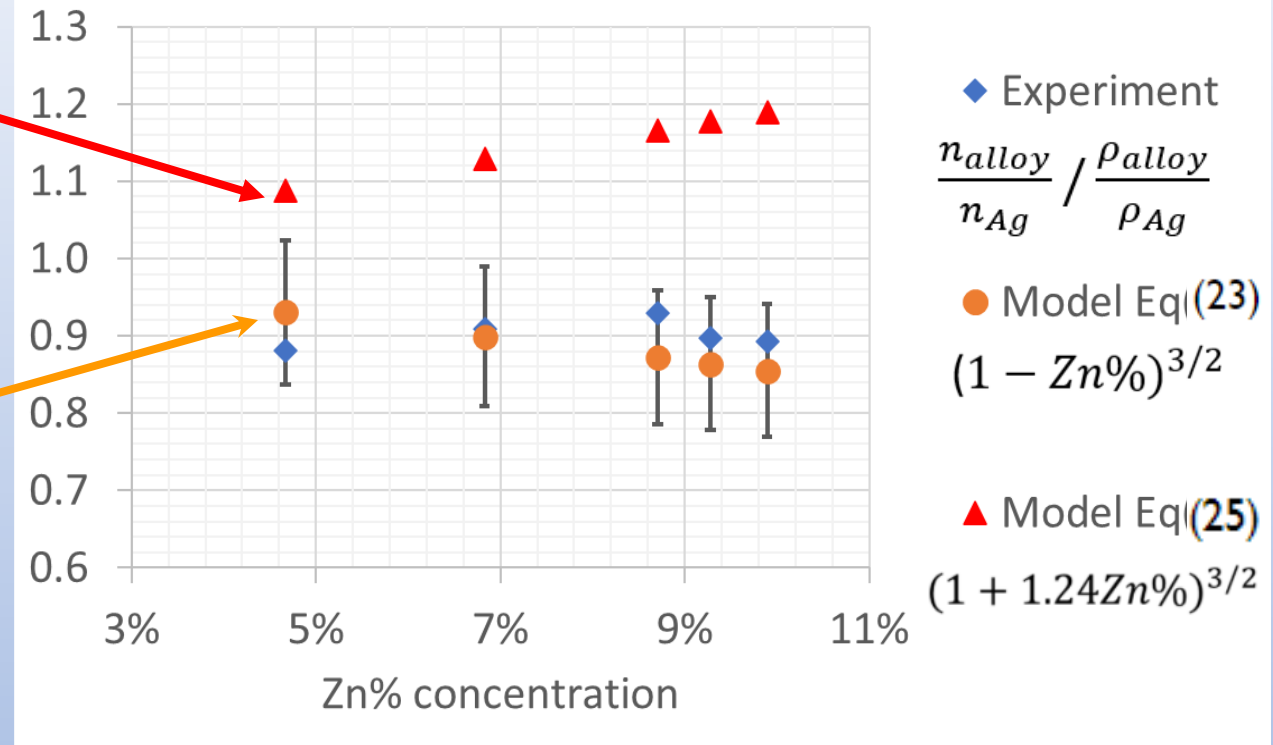
$$\frac{n_{alloy}}{n_{Ag}} / \frac{\rho_{alloy}}{\rho_{Ag}} = (1 - Zn\%)^{3/2} \quad \checkmark \quad (23)$$

- In conclusion, Zn contributes no free electrons

- Error bar discussion. $< \pm 12\%$

- Calculated from the sum of all standard deviations of measurements of ρ ratios $< 5\%$
- plus the deposition n_{Ag} and n_{alloy} ratio variation of $< 7\%$,

Model vs experiment results comparison



Runsheets Summary

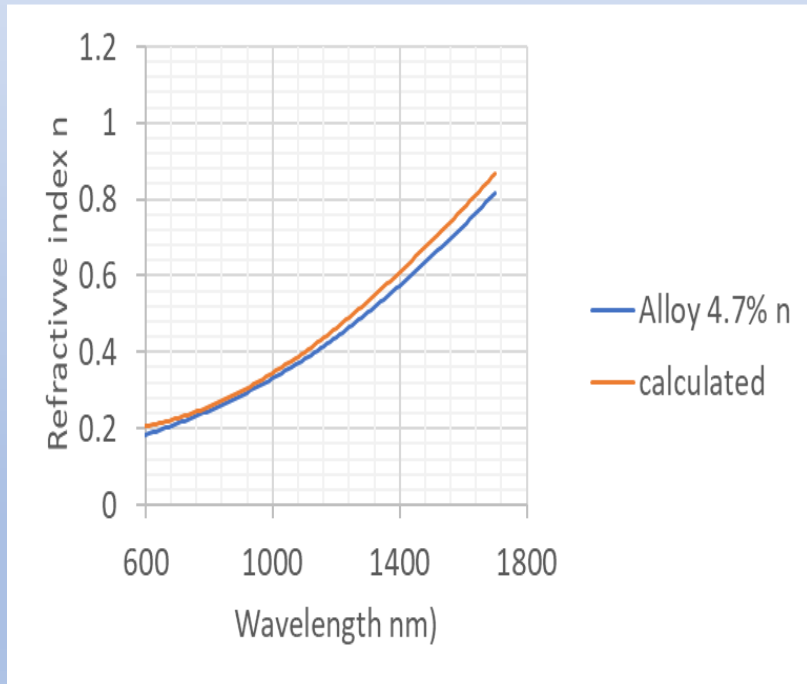
run #	Zinc power	Ag power	pressure (mT)	Ar flow (sccm)	Time Sec	thickness (nm)	Dep Rate (nm/s)	average Rs (ohm)	SteEV	1sigma	Resistivity (ohm*m)	Zn% in volume	alloy electron density (/m3)	collision time τ (s)	wavelength λ for $(\omega\tau)^2 \gg 1$ (nm)	plasma frequency (Hz)	wavelength λ (nm) for $(\omega_{pe}/\omega)^2 \gg 1$
D71-3		100w	2.5	360	70	26.4	0.38	1.4	2.5%	1.9%	3.6E-08	0	5.80E+28	1.71E-14	1.02E+04	1.36E+16	4.38E+02
D71-7	6w	100W	2.5	360	70	29.1	0.42	3.8	4.5%	1.2%	1.1E-07	9.3%	5.26E+28	6.09E-15	3.63E+03	1.29E+16	4.60E+02
D72-1		150W	2.5	360	60	34.1	0.57	1.0	2.2%	2.2%	3.4E-08	0	5.80E+28	1.80E-14	1.07E+04	1.36E+16	4.38E+02
D72-3	6w	150W	2.5	360	60	36.6	0.61	2.7	2.8%	1.0%	9.9E-08	6.8%	5.40E+28	6.65E-15	3.96E+03	1.31E+16	4.54E+02
D72-5		200W	2.5	360	45	34.7	0.77	1.1	1.9%	1.8%	3.7E-08	0	5.80E+28	1.66E-14	9.91E+03	1.36E+16	4.38E+02
D72-7	6w	200W	2.5	360	45	36.4	0.81	2.2	2.0%	0.9%	7.9E-08	4.7%	5.53E+28	8.10E-15	4.82E+03	1.33E+16	4.49E+02
D73-1		100W	2.5	360	90	34.6	0.38	1.0	3.0%	3.0%	3.5E-08	0	5.80E+28	1.77E-14	1.05E+04	1.36E+16	4.38E+02
D73-5	6w	100W	2.5	360	90	37.9	0.42	2.9	2.7%	0.9%	1.1E-07	8.7%	5.29E+28	6.19E-15	3.69E+03	1.30E+16	4.59E+02
D73-7	6w	100W	2.5	360	90	38.4	0.43	2.8	4.4%	1.5%	1.1E-07	9.9%	5.23E+28	6.26E-15	3.73E+03	1.29E+16	4.62E+02

- 3 different Zn% of AgZn alloy were studied by co-sputter method,
- To meet our assumptions, we need the wavelength to be at least greater than 600nm and smaller than 3000nm:
 - Assumption 3: $\omega^2 \tau^2 \gg 1$; Valid for wavelength $< 3\mu m$
 - Assumption 4: $\omega_{pe}^2 \gg \omega^2$: valid for wavelength $> 0.6 \mu m$

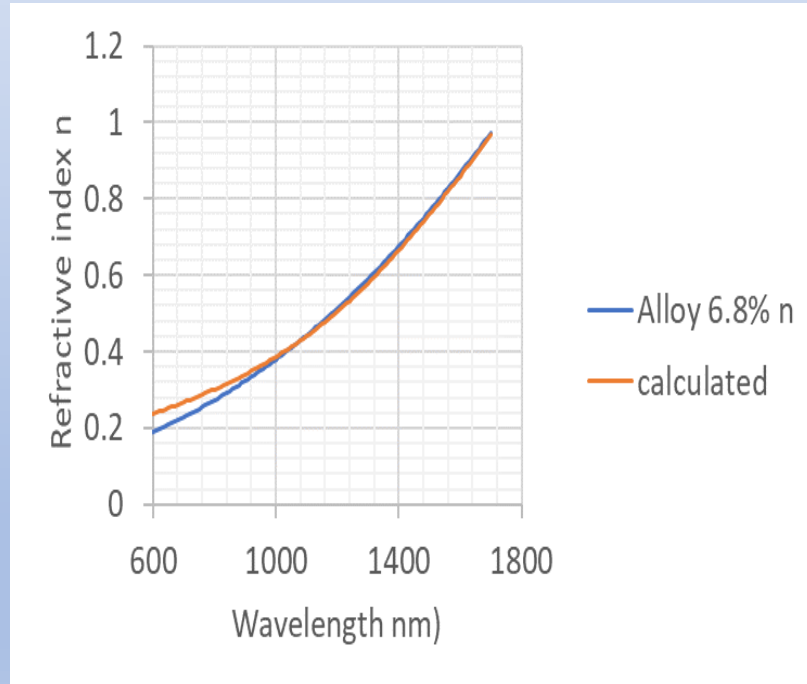
Alloy index model calculation vs experiment measurements

$$\text{Alloy Index : } n_{\text{alloy}} = (1 - \text{Zn}\%)^{3/2} * \frac{\rho_{\text{alloy}}}{\rho_{\text{Ag}}} * n_{\text{Ag}} \quad (26)$$

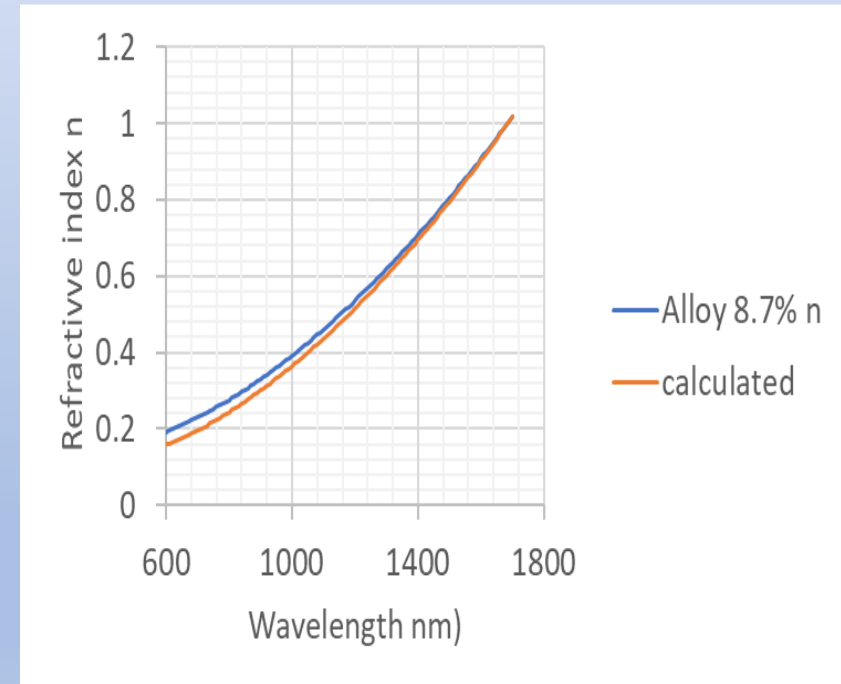
AgZn (Zn 4.7%)



AgZn (Zn 6.8%)



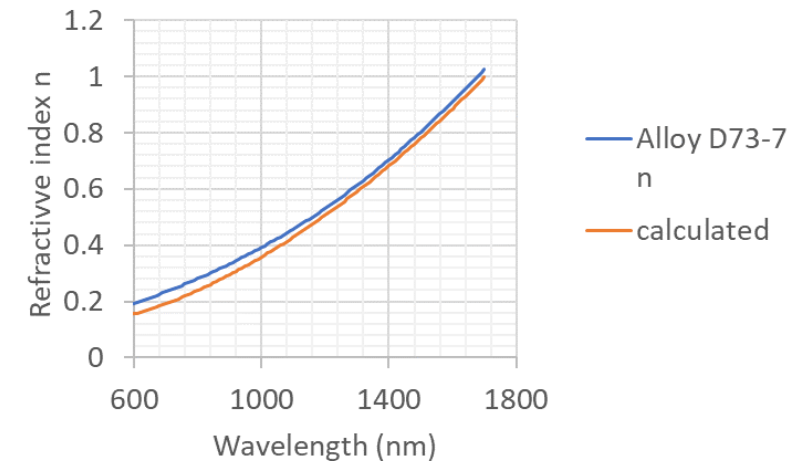
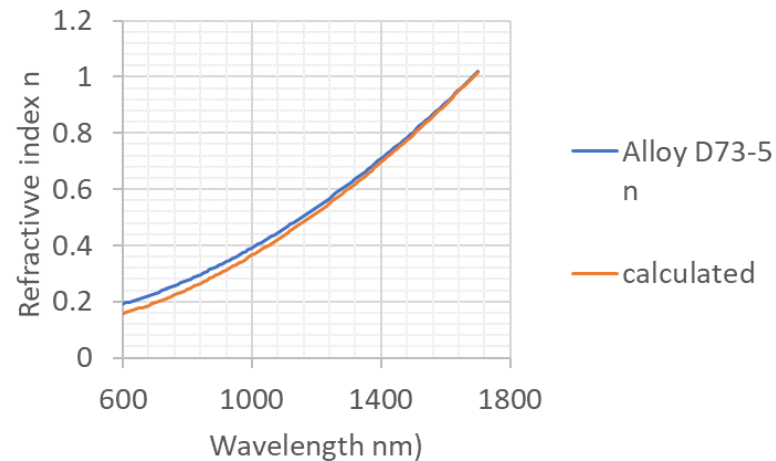
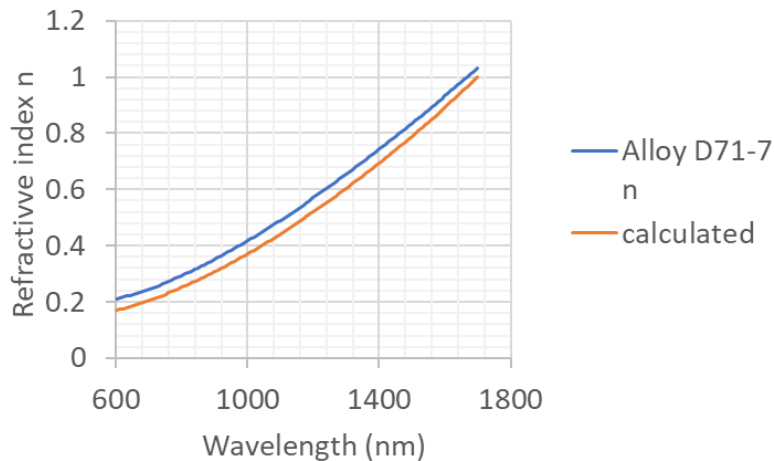
AgZn (Zn 8.7%)



The model calculations and the experiment results match up well

Repeatability study:

- Indexes ratio variation from three model calculation showed $\sim 7\%$ standard deviation in average of the spectra.
 - Two Silver depositions of 100W with $<4\%$ index variation
 - Three Alloy depositions of 100W Ag + 6 W Zn with $<3\%$ index variation



Repeated Silver alloy index of 100wAg + 6W Zn and the calculation from the theory eq. (26)

Conclusions

- We theoretically derived a refractive index calculation that depends only on two parameters which canceled out other factors.

$$\frac{n_{alloy}}{n_{Ag}} = \frac{n_{e-alloy}^{3/2} * \rho_{alloy}}{n_{e-Ag}^{3/2} * \rho_{Ag}}$$

- Valid experimental conditions were confirmed between 0.6 μm and 3 μm
- Alloy index with concentration relationship was derived:
$$n_{alloy} = (1 - Zn\%)^{3/2} * \frac{\rho_{alloy}}{\rho_{Ag}} * n_{Ag}$$
 - Theory and experiments agree within error bar
 - Experimentally confirmed that Zn contributes no free electrons in alloy AgZn film properties in this study.

Future study on why Zn does not contribute free electron in AgZn alloy?

- This study indicated that Zn does not contribute free electron in AgZn alloy.
- Literature report AgGe with alloy concentration 26%-37%, the 2nd element Ge contribute free electrons
- However, there are literature of AgFe with 1%, AlCu(0.5%-1.5%)alloy free electrons are lower than the pure silver concentration, which means the 2nd element is likely not contribute free electron.
- Our hypothesis is: at very low concentration of alloy element in a highly conducting metal silver, the electrons from the 2nd element is localized and is not able to contribute any free electrons to the conducting current.
- Any suggestion?

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